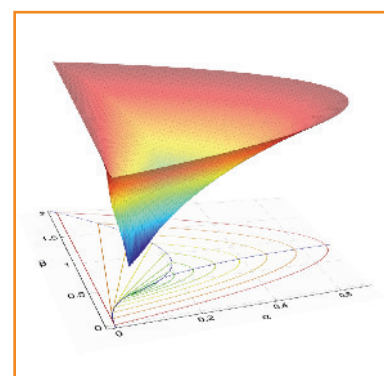
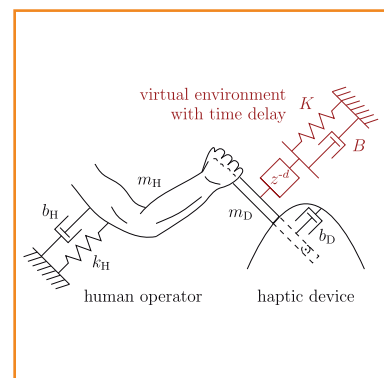


Thomas Hulin

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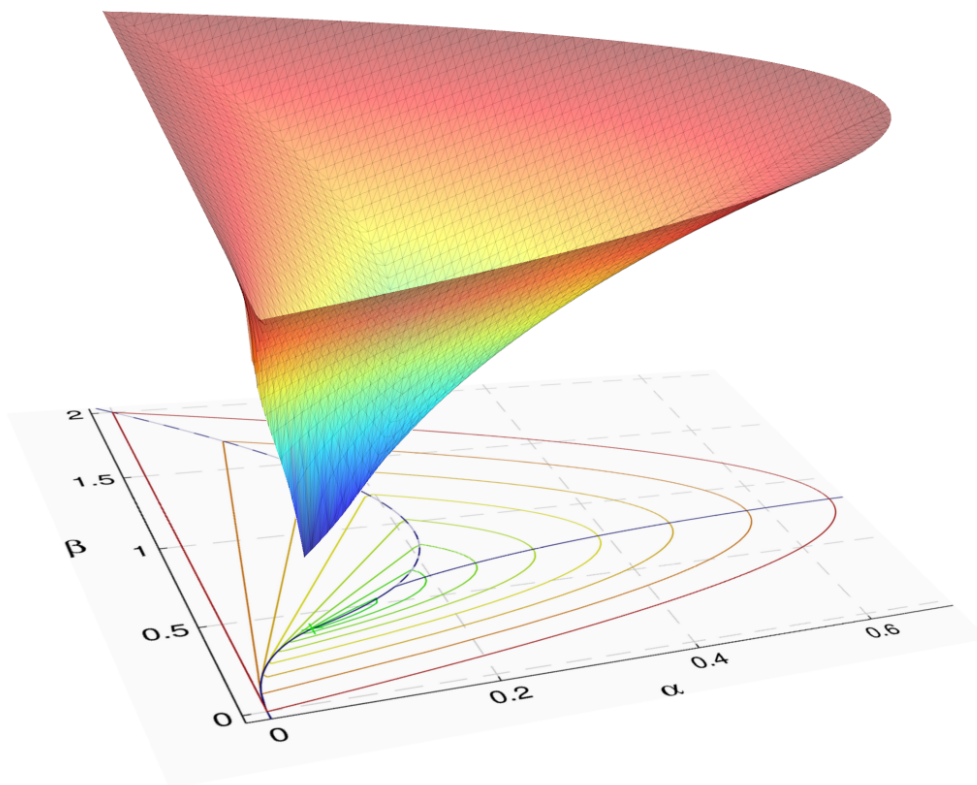
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der Gottfried Wilhelm Leibniz Universität Hannover
zur Erlangung des akademischen Grades
Doktor-Ingenieur
genehmigte Dissertation

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Dipl.-Ing. Thomas Hulin



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Preface

Interacting with a virtual environment without perceiving haptic feedback is like eating without smelling the delicious fragrance of the food or watching a movie without hearing its impressive sound effects. Researching on haptic feedback has been my main research interest in the past years, since I started my work as a young researcher at the Institute of Robotics and Mechatronics. This thesis summarizes important results of my research on haptic control carried out at the Institute of Robotics and Mechatronics at the DLR (German Aerospace Center). I have already published parts of this work within several conference and journal papers and the present thesis contains text passages from these publications. The introductory sections of the respective chapters contain appropriate references accordingly.

It is important to me to mention that the findings of my research do not only apply to haptic systems but in fact to a wide variety of physical systems. This is mainly due to electromechanical analogies [13] and the analytical representation of the investigated hybrid control system. Hence, I hope that my findings will also inspire and advance the research in domains other than haptics. To this end, I tried to present the results as clear as possible in an understandable language with numerous meaningful figures, and I want to motivate other researchers to also put emphasis on a clear and comprehensible form of presentation of their research activities.

A lot of people supported me in conducting my research and made this thesis possible. In particular, I would like to express my gratitude to the following people for their valuable and constructive support. First of all, I would like to thank Professor Gerhard Hirzinger, the former head of the institute, who largely founded this great institute and who managed to create an amazingly inspiring working atmosphere. My particular thanks go also to Professor Alin Albu-Schäffer, the head of the DLR's Institute of Robotics and Mechatronics, who understands well how to motivate his colleagues in publishing their research activities and writing doctoral theses. Christian Ott, the head of the department for Analysis and Control of Advanced Robotic Systems, created the freedom for me to work on my research topics and to finalize the thesis. It is a great privilege to work in this institute and in this research department.

I want to thank Professor Jürgen Ackermann and Naim Bajcinca, who introduced me into the fascinating field of parameter space control design during my diploma thesis under their supervision. I have learned a lot during these few months of work and, more importantly, the interest in this topic has never left me since. Professor Tobias Ortmaier deserves my special thanks for supervising my doctoral studies and

providing valuable advices for improving the thesis.

I want to express my particular gratitude to Carsten Preusche for establishing the research group for telepresence and virtual reality, of which I have been a member since I started working at DLR. He inspired my work with a remarkable number of various ideas. My special thanks go also to the whole research group for telepresence and virtual reality, and all the colleagues that were involved in building the amazing robotic systems that I could use for conducting my research work.

I gratefully acknowledge the fruitful and constructive collaboration with Bernhard Vodermayr in the international research project STAMAS. My sincere thanks also go to my office mates Joseph Reill, Andreas Tobergte, and Phillip Schmidt, who often had to listen to my desperation and who encouraged me in finalizing my thesis. I also thank all my students in supporting me in my research activities. The reviewers and editors of my scientific publications also deserve my gratitude, as they provided valuable input and excellent suggestions for improvements.

My special thanks go to Jorge Juan Gil, who shared with me his extensive experience and knowledge in the field of stable haptic control and who get never tired to discuss on control issues. I have learned a lot from him during the six months that he was visiting our institute as a guest scientist, and also afterwards during numerous short visits and intense discussions.

There are three persons to whom I want to express my sincerest gratitude: Philipp Kremer, Katharina Hertkorn, and Mikel Sagardia, who proofread this thesis and also motivated and pushed me to finalize it. They had invested hours of their time and I sincerely appreciate their excellent ideas and comments. Also, my grateful thanks go to Anja Hellings and Phillip Schmidt for proofreading parts of this thesis.

I want to express my gratitude to the VR-Lab of the Volkswagen AG, which funded a research project on haptic assembly simulations. I also acknowledge the support from the EU for funding three research projects that I have worked on, in particular ENACTIVE (IST-2004-002114), SKILLS (FP6-IST-035005), and STAMAS (Project reference: 312815). Finally, I would like to thank the reader in advance for taking the time to read this thesis and I am convinced that the time spent is a worthwhile investment.

Oberpfaffenhofen, January 2017

Thomas Hulin

The pictures on the cover page show (i) the haptic device HUG that was used for the experiments (photo: DLR, CC-BY 3.0), (ii) the investigated model, and (iii) a three-dimensional illustration of the left contour plot of Fig. 5.2. The lower tip of this three dimensional-shape is the optimum point with respect to the pole-based settling time.

Abstract

Haptic rendering denotes the process of computing and displaying forces from a virtual environment to a human operator via a haptic device. From the control point of view, the haptic system comprising virtual environment, haptic device, and human operator is a hybrid control system that contains both discrete- and continuous-time elements. Discrete-time sampling as well as time delay that is typically present in such haptic systems may lead to unstable behavior.

This thesis investigates stability, passivity, and control design of such hybrid system. Its primary goal is to close some of the existing lacks in the current state of research, in particular to analyze the influence of the human operator on a haptic system behavior, to investigate the precise effect of delay and discrete-time sampling, and to introduce optimal control methods to the field of haptic rendering. A unique characteristic of the presented approach is the exact combination of discrete- and continuous-time elements, while taking into account time delay and user dynamics.

A linear stability analysis is presented to determine the stability boundaries of the haptic system and to investigate the influence of both delay and human operator. This analysis leads to the definition of normalized dimensionless parameters greatly simplifying calculations and presentation of results. The analysis reveals that the human operator modeled as mass-spring-damper system has a stabilizing effect, which is mainly constituted by its mass contribution. For small parameter values of the virtual environment, the relationship between the parameters may be approximated by a linear stability condition.

Passivity is analyzed by enhancing an existing passivity approach towards delayed haptic systems. The influence of the system parameters on passivity is completely different than for stability. For realistic parameter values, passive regions result as small subregions of the stable regions, which emphasizes the fact that passivity is highly conservative with regard to stability. This is because passivity admits human arm stiffnesses that are orders of magnitudes higher than realistically feasible.

To analyze the performance of a haptic system, various optimization criteria are investigated that are either based on the system poles or on the transient response. Each of these criteria is based on a dimensionless performance measure resulting in cost maps and in optimal points that hold for any positive mass and sampling rate. A polynomial approximation function is found to predict the optimal performance of the haptic system in these optimal points under the influence of delay. This function leads to the formulation of an easy-to-remember rule of thumb for the optimal settling time.

The theoretical investigations are accompanied by a series of experiments on two different devices, a Novint Falcon and a DLR/KUKA light-weight robot. They exhibit a remarkable accordance to the theoretical results. The practical impact of this thesis on haptic rendering applications was already demonstrated in haptic assembly simulations and haptically supported training. In addition, the theoretical results lead to design guidelines of haptic devices and provide the theoretical basis for future psychophysical studies.

Keywords: haptic rendering, time delay, stability analysis, passivity analysis, optimal control

Kurzfassung

Titel der Arbeit: Regelung totzeitbehafteter hybrider Systeme mit Anwendung für haptisches Rendern

Haptisches Rendern beschreibt die Berechnung von Kräften aus der virtuellen Welt und deren Darstellung an den Menschen über ein haptisches Gerät. Aus regelungstechnischer Sicht ist das haptische System bestehend aus virtueller Umgebung, haptischem Gerät und dem Menschen ein hybrides System, das sowohl zeitdiskrete als auch zeitkontinuierliche Elemente enthält. Die zeitdiskrete Abtastung sowie eine zusätzliche Totzeit, die typischerweise in solchen haptischen Systemen vorhanden ist, können zu einem instabilen Systemverhalten führen.

Diese Dissertationsschrift untersucht Stabilität, Passivität und den Reglerentwurf für solche hybriden Systeme. Das primäre Ziel dieser Arbeit ist es einige grundlegende Lücken im Stand der Forschung auf diesem Gebiet zu schließen. Im einzelnen wird der Einfluss des Menschen auf das Verhalten haptischer Systeme analysiert, die genaue Auswirkung von Totzeit und zeitdiskreter Abtastung untersucht und Methoden der optimalen Regelung in das Gebiet des haptischen Renderns eingeführt. Ein Alleinstellungsmerkmal des vorgestellten Ansatzes ist die exakte Kombination von zeitdiskreten und -kontinuierlichen Elementen unter gleichzeitiger Berücksichtigung von Totzeit und der Dynamik des Benutzers.

In einer linearen Stabilitätsanalyse werden die Stabilitätsgrenzen des haptischen Systems bestimmt und untersucht, wie sie sich durch die Totzeit und den Benutzer verändern. Die Analyse führt zu normierten, dimensionslosen Parametern, mit denen sich die Berechnungen stark vereinfachen lassen und die eine klare Präsentation der Ergebnisse ermöglichen. Sie offenbart auch, dass der Mensch, als Masse-Feder-Dämpfer System modelliert, stabilisierend auf das haptische System wirkt, was hauptsächlich an der zusätzlich eingebrachten Trägheit liegt. Für kleine Parameterwerte der virtuellen Wand kann das Verhältnis zwischen den Parametern durch eine lineare Stabilitätsbedingung angenähert werden.

Passivität wird unter Verwendung eines existierenden Passivitätsansatzes für haptische Systeme analysiert, der dazu bezüglich Totzeiten verallgemeinert wird. Es zeigt sich, dass sich der Einfluss der Systemparameter auf Passivität strukturell von dem für Stabilität unterscheidet. Für realistische Parameterwerte resultieren darüber hinaus die passiven Parametergebiete als Teile der stabilen Gebiete. Dies unterstreicht die Tatsache, dass Passivität stark konservativ bezüglich Stabilität ist. Der Grund dafür liegt in dem von der Passivitätsanalyse betrachteten Steifigkeitsbereich des menschlichen

Arms, der realistische Werte um Größenordnungen übersteigt.

Die Performanz haptischer Systeme wird anhand verschiedenartiger Optimierungskriterien untersucht, die entweder auf der Lage der Systempole oder auf dem Einschwingverhalten basieren. Für jedes dieser Kriterien wird ein dimensionsloses Performanzmaß eingeführt, mit welchem Kostenkarten und optimale Punkte berechnet werden können, die unabhängig von der Masse und der Abtastrate sind. Mit Hilfe einer polynomischen Approximationsfunktion lässt sich die optimale Performanz des haptischen Systems unter dem Einfluss der Totzeit vorhersagen. Diese Funktion führt außerdem zu einer leicht zu merkenden Faustregel für die optimale Einschwingzeit.

Die theoretischen Untersuchungen werden von einer Reihe an Experimenten an zwei unterschiedlichen Geräten begleitet, einem Novint Falcon und einem DLR/KUKA Leichtbauroboter. Sie weisen bemerkenswerte Übereinstimmungen zu den theoretischen Ergebnissen auf. Der praktische Nutzen der in dieser Dissertationsschrift neu vorgestellten Erkenntnisse konnte bereits erfolgreich in zwei Anwendungen demonstriert werden, in einer haptischen Einbausimulation und in haptisch unterstütztem Training. Darüber hinaus führen die theoretischen Ergebnisse zu Gestaltungsrichtlinien für haptische Geräte und liefern die theoretische Grundlage für zukünftige psychophysische Studien.

Schlagnote: haptisches Rendern, Totzeit, Stabilitätsanalyse, Passivitätsanalyse, optimale Regelung

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Notations

List of Abbreviations

Table 1: Abbreviations

abbreviation	description
BIBO stability	bounded input-bounded output stability
CAD	computer-aided design
DLR	German Aerospace Center
DoF	degree of freedom
ISE	integral of the square of the error
ITSE	integral of time multiplied by the squared error
ISTSE	integral of squared time multiplied by the squared error
LWR	Light-Weight Robot
VR	virtual reality
ZOH	zero-order hold

List of Mathematical Abbreviations

Table 2: Mathematical abbreviations

operator	description
$\cos(\cdot)$	cosine function
$\deg(\cdot)$	degree of a polynomial
$\ln(\cdot)$	natural logarithm
$\max(\cdot)$	maximum of a set or function
$\min(\cdot)$	minimum of a set or function
$\sin(\cdot)$	sine function

Conventions

Throughout this dissertation, italic letters indicate scalars while vectors and matrices are denoted by bold letters. Dots denote derivatives with respect to time t .

Table 3: Subscripts and superscripts

sub-/superscripts	description
x_D	parameter x associated with the haptic device
x_E	parameter x associated with an energy
x_F	parameter x associated with a force
x_H	parameter x associated with the human operator
x_k	parameter x at time instant $t = k \cdot T$ with $k \in \mathbb{N}_0$
x_{\max}	maximum value of parameter x
x_{obs}	observed value of parameter x
x_{opt}	optimal value of parameter x
x_{ov}	parameter x associated with the relative overshoot
x_{rot}	parameter x for a rotational movement
x_{settle}	parameter x associated with system settling time
x_x	parameter x associated with a position
x_0	initial or specific value of parameter x
x_∞	abbreviation for $\lim_{t \rightarrow \infty} x(t)$
x^*	discrete-time sampled signal of a parameter x
O^{step}	optimization criterion based on the step response
O^{impulse}	optimization criterion based on the impulse response

List of Symbols

The following table summarizes the symbols that are used in this thesis. Their units are also given in the last column, where dashes (–) stand for dimensionless parameters and stars (*) marks ambiguous parameters units. The units for the rotational case are given in parentheses, if applicable.

Table 4: Symbols

symbol	description	unit
b	physical damping	Ns/m (Nms/rad)
B	virtual damping	Ns/m (Nms/rad)
c_i	substitution variable	–
C	cost function	–
d	delay factor	–
$\delta(\cdot)$	Dirac delta function	–
e	Euler's number	–

E	energy	Nm
F	force	N
$\mathcal{F}(\cdot)$	Fourier transform	*
g	slope of a function	–
$G_x(\cdot)$	closed-loop transfer function with output parameter x	*
$H_x(\cdot)$	open-loop transfer function with output parameter x	*
I	moment of inertia	kg·m ²
j	imaginary unit	–
k	physical stiffness	N/m (Nm/rad)
K	virtual stiffness	N/m (Nm/rad)
$l(\cdot)$	function of a line	–
m	mass	kg
$n(\cdot)$	polynomial in the numerator of a transfer function	*
O	optimization criterion	–
$p(\cdot)$	characteristic polynomial of a transfer function	*
r	radius of a concentric circle in the complex z -plane	–
\Re	real part of a complex argument	*
s	Laplace variable	1/s
t	time	s
t_d	time delay	s
t_r	effective time delay	s
T	sampling period	s
$u(\cdot)$	unit step function or Heaviside step function	–
w	weighting factor or exponent	–
x	position	m
z	Z-transform variable	–
\mathcal{Z}	Z-transform	*
α	normalized virtual stiffness	–
β	normalized virtual damping	–
γ	normalized physical stiffness	–
δ	normalized physical damping	–
ϵ	arbitrarily small positive quantity	*
ζ	system damping ratio	–
η	ratio of two parameters	–
Θ	joint angle	rad
κ	integer time index of discrete-time systems	–
ρ	relative error	–
τ	variable of integration representing time	s
τ	torque	Nm
χ	weighted position	N (Nm)
ω	angular frequency	rad/s
ω_N	Nyquist frequency	rad/s

Bibliography

- [1] K. J. Åström and R. M. Murray. *Feedback Systems: An Introduction for Scientists and Engineers*. Princeton University Press, September 2012.
- [2] K. J. Åström and B. Wittenmark. *Computer-Controlled Systems: Theory and Design*. Prentice Hall, 3rd edition, 1997.
- [3] K. J. Åström and B. Wittenmark. *Adaptive Control*. Addison-Wesley, 2nd edition, 2008.
- [4] J. J. Abbott and A. M. Okamura. Effects of position quantization and sampling rate on virtual-wall passivity. *IEEE Trans. on Robotics*, 21(5):952–964, October 2005.
- [5] J. Ackermann. *Sampled-Data Control Systems: Analysis and Synthesis, Robust System Design*. Springer Science & Business Media, 2012.
- [6] J. Ackermann, P. Blue, T. Bünte, L. Güvenc, D. Kaesbauer, M. Kordt, M. Muhler, and D. Odenthal. *Robust Control: The Parameter Space Approach*. Communications and Control Engineering Series. Springer-Verlag GmbH, 2002.
- [7] R. J. Adams and B. Hannaford. Stable haptic interaction with virtual environments. *IEEE Trans. on Robotics and Automation*, 15(3):465–474, June 1999.
- [8] R. J. Adams and B. Hannaford. Control law design for haptic interfaces to virtual reality. *IEEE Trans. on Control Systems Technology*, 10(1):3–13, January 2002.
- [9] N. Bajcinca and T. Hulin. RobSin: A new tool for robust design of pid and three-term controllers based on singular frequencies. In *IEEE Int. Conf. on Control Applications*, volume 2, pages 1546–1551. IEEE, 2004.
- [10] N. Bajcinca and T. Hulin. Menge aller robust stabilisierenden PID-Regler: Methodik und Software (Teil I–III). *at - Automatisierungstechnik*, 2005–2006.
- [11] C. Basdogan and M. A. Srinivasan. Haptic rendering in virtual environments. In K.M. Stanney, editor, *Handbook of Virtual Environments: Design, Implementation, and Applications*, pages 117–134. Erlbaum, 2002.

- [12] A. Bicchi, M. Buss, M.O. Ernst, and A. Peer. *The Sense of Touch and its Rendering: Progress in Haptics Research*. Springer, Berlin, Germany, 2008.
- [13] A. Bloch. Electromechanical analogies and their use for the analysis of mechanical and electromechanical systems. *Electrical Engineers - Part I: General, Journal of the Institution of*, 92(52):157–169, April 1945.
- [14] T. L. Brooks. Telerobotic response requirements. In *IEEE Trans. on Systems, Man, and Cybernetics*, pages 113–120, Los Angeles, CA, November 1990.
- [15] J. Buchli, F. Stulp, E. Theodorou, and S. Schaal. Learning variable impedance control. *The Int. Journal of Robotics Research*, 30(7):820–833, November 2011.
- [16] M. C. Cavusoglu, D. Feygin, and F. Tendick. A critical study of the mechanical and electrical properties of the PHANToM haptic interface and improvements for high performance control. *Presence*, 11(6):555–568, 2002.
- [17] V. Chawda, O. Celik, and M. K. O'Malley. A method for selecting velocity filter cut-off frequency for maximizing impedance width performance in haptic interfaces. *ASME Journal of Dynamic Systems, Measurement, and Control*, 137(2):024503, February 2015.
- [18] J. Y. C. Chen and J. E. Thropp. Review of low frame rate effects on human performance. *IEEE Trans. on Systems, Man, and Cybernetics*, 37(6):1063–1076, 2007.
- [19] D. Christiansen and C. Alexander. *Standard Handbook of Electronic Engineering*. McGraw-Hill Education, 5th edition, 2005.
- [20] P. Ciáurriz, I. Díaz, and J. J. Gil. Stable discrete-time impedances for haptic systems with vibration modes and delay. *IEEE Trans. on Control Systems Technology*, 22(3):884–895, May 2014.
- [21] J. E. Colgate and J. M. Brown. Factors affecting the z-width of a haptic display. In *IEEE Int. Conf. on Robotics and Automation (ICRA)*, pages 3205–3210, May 1994.
- [22] J. E. Colgate and N. Hogan. An analysis of contact instability in terms of passive physical equivalents. In *IEEE Int. Conf. on Robotics and Automation (ICRA)*, pages 404–409, Scottsdale, AZ, USA, May 1989.
- [23] J. E. Colgate and G. Schenkel. Passivity of a class of sampled-data systems: Application to haptic interfaces. In *1994 American Control Conference*, pages 37–47. AIAA, 1994.

- [24] J. E. Colgate and G. Schenkel. Passivity of a class of sampled-data systems: Application to haptic interfaces. *Journal of Robotic Systems*, 14(1):37–47, January 1997.
- [25] J. E. Colgate, M. C. Stanley, and J. M. Brown. Issues in the haptic display of tool use. In *IEEE/RSJ Int. Conf. on Intelligent Robots and Systems (IROS)*, volume 3, pages 140–145, Pittsburgh, PA, USA, Aug 1995.
- [26] J. J. Craig. *Introduction to Robotics Mechanics and Control*. Addison-Wesley Publishing Company, Inc., USA, 2nd edition, 1989.
- [27] Q. V. Dang, A. Dequidt, L. Vermeiren, and M. Dambrine. Experimental study on stability of a haptic system with variable time delays. In *IEEE/ASME Int. Conf. on Advanced Intelligent Mechatronics (AIM)*, pages 554–559, July 2014.
- [28] Q. V. Dang, L. Vermeiren, A. Dequidt, and M. Dambrine. Analyzing stability of haptic interface using linear matrix inequality approach. In *IEEE Int. Conf. on Robotics and Biomimetics*, pages 1129–1134, December 2012.
- [29] R. W. Daniel and P. R. McAree. Fundamental limits of performance for force reflecting teleoperation. *The Int. Journal of Robotics Research*, 17(8):811–830, August 1998.
- [30] I. Díaz and J. J. Gil. Influence of internal vibration modes on the stability of haptic rendering. In *IEEE Int. Conf. on Robotics and Automation (ICRA)*, pages 2884–2889, Pasadena, CA, May 2008.
- [31] I. Díaz, J. J. Gil, and T. Hulin. *Advances in Haptics*, chapter Stability Boundary and Transparency for Haptic Rendering, pages 103–125. INTECH, 2010.
- [32] I. Diaz and J.J. Gil. Influence of vibration modes and human operator on the stability of haptic rendering. *IEEE Trans. on Robotics*, 26(1):160–165, February 2010.
- [33] N. Diolaiti, G. Niemeyer, F. Barbagli, and J. K. Salisbury. Stability of haptic rendering: Discretization, quantization, time delay, and coulomb effects. *IEEE Trans. on Robotics*, 22(2):256–268, April 2006.
- [34] G. F. Franklin, J. D. Powell, and M. L. Workman. *Digital Control of Dynamic Systems*. Addison-Wesley, Menlo Park, 3rd edition, 1998.
- [35] J. J. Gil, A. Avello, Á. Rubio, and J. Flórez. Stability analysis of a 1 DOF haptic interface using the Routh-Hurwitz criterion. *IEEE Trans. on Control Systems Technology*, 12(4):583–588, July 2004.

- [36] J. J. Gil, E. Sánchez, T. Hulin, C. Preusche, and G. Hirzinger. Stability boundary for haptic rendering: Influence of damping and delay. In *IEEE Int. Conf. on Robotics and Automation (ICRA)*, Rome, Italy, April 2007.
- [37] J. J. Gil, E. Sánchez, T. Hulin, C. Preusche, and G. Hirzinger. Stability boundary for haptic rendering: Influence of damping and delay. *Journal of Computing and Information Science in Engineering*, 9(1):011005–1–011005–8, March 2009.
- [38] R. B. Gillespie and M. R. Cutkosky. Stable user-specific haptic rendering of the virtual wall. In *1996 International Mechanical Engineering Congress and Exhibition*, volume 58, pages 397–406, Atlanta, November 1996.
- [39] A. H. C. Gosline and V. Hayward. Time-domain passivity control of haptic interfaces with tunable damping hardware. In *IEEE World Haptics Conference (WHC)*, pages 164–169, March 2007.
- [40] D. Graham and R. C. Lathrop. The synthesis of optimum transient response: Criteria and standard forms. *Trans. of the AIEE, Part II: Applications and Industry*, 72(5):273–288, November 1953.
- [41] G. Habib, G. Rega, and G. Stepan. Stability analysis of a two-degree-of-freedom mechanical system subject to proportional–derivative digital position control. *Journal of Vibration and Control*, 21(8):1539–1555, April 2015.
- [42] B. Hannaford and J.-H. Ryu. Time-domain passivity control of haptic interfaces. *IEEE Trans. on Robotics and Automation*, 18(1):1–10, February 2002.
- [43] V. Hayward, O. R. Astley, M. Cruz-Hernandez, D. Grant, and G. Robles-De-La-Torre. Haptic interfaces and devices. *Sensor Review*, 24(1):16–29, 2004.
- [44] V. Hayward and K. E. MacLean. Do it yourself haptics, part-i. *IEEE Robotics and Automation Magazine*, 14(4):88–104, December 2007.
- [45] K. Hertkorn, T. Hulin, P. Kremer, C. Preusche, and G. Hirzinger. Time domain passivity control for multi-degree of freedom haptic systems with time delay. In *IEEE Int. Conf. on Robotics and Automation (ICRA)*, pages 1313–1319, Anchorage, Alaska, USA, May 2010.
- [46] G. Hirzinger, N. Sporer, M. Schedl, J. Butterfaß, and M. Grebenstein. Torque-controlled lightweight arms and articulated hands: Do we reach technological limits now? *The Int. Journal of Robotics Research*, 23(4-5):331–340, June 2004.
- [47] N. Hogan. Controlling impedance at the man/machine interface. In *IEEE Int. Conf. on Robotics and Automation (ICRA)*, volume 3, pages 1626–1631, Scottsdale, AZ, USA, May 1989.

- [48] T. Hulin, A. Albu-Schäffer, and G. Hirzinger. Passivity and stability boundaries for haptic systems with time delay. *IEEE Trans. on Control Systems Technology*, 22(4):1297–1309, July 2014.
- [49] T. Hulin, J. J. Gil, E. Sánchez, C. Preusche, and G. Hirzinger. Experimental stability analysis of a haptic system. In *Int. Conf. on Enactive Interfaces*, pages 157–158, Montpellier, France, November 2006.
- [50] T. Hulin, R. González Camarero, and A. Albu-Schäffer. Optimal control for haptic rendering: Fast energy dissipation and minimum overshoot. In *IEEE/RSJ Int. Conf. on Intelligent Robots and Systems (IROS)*, pages 4505–4511, Tokyo, Japan, November 2013.
- [51] T. Hulin, K. Hertkorn, P. Kremer, S. Schätzle, J. Artigas, M. Sagardia, F. Zacharias, and C. Preusche. The DLR bimanual haptic device with optimized workspace. In *IEEE Int. Conf. on Robotics and Automation (ICRA)*, pages 3441–3442, Shanghai, China, May 2011.
- [52] T. Hulin, K. Hertkorn, and C. Preusche. Interactive features for robot viewers. In *Int. Conf. on Intelligent Robotics and Applications (ICIRA)*, pages 181–193, Montreal, Canada, October 2012.
- [53] T. Hulin, C. Preusche, and G. Hirzinger. Haptic rendering for virtual assembly verification (poster). In *IEEE World Haptics Conference (WHC)*, Pisa, Italy, March 2005.
- [54] T. Hulin, C. Preusche, and G. Hirzinger. Stability boundary and design criteria for haptic rendering of virtual walls. In *Int. IFAC Symp. on Robot Control (SYROCO)*, Bologna, Italy, September 2006.
- [55] T. Hulin, C. Preusche, and G. Hirzinger. Stability boundary for haptic rendering: Influence of physical damping. In *IEEE/RSJ Int. Conf. on Intelligent Robots and Systems (IROS)*, pages 1570–1575, Beijing, China, October 2006.
- [56] T. Hulin, C. Preusche, and G. Hirzinger. Stability boundary for haptic rendering: Influence of human operator. In *IEEE/RSJ Int. Conf. on Intelligent Robots and Systems (IROS)*, pages 3483–3488, Nice, France, September 2008.
- [57] T. Hulin, C. Preusche, E. Yechiam, A. Telpaz, V. Schmirgel, and U. E. Zimmermann. Haptic and visual training of system behavior—a case study for robotic programming-by-demonstration. In *The International SKILLS Conference*, Montpellier, France, December 2011.
- [58] T. Hulin, M. Sagardia, J. Artigas, S. Schätzle, P. Kremer, and C. Preusche. Human-scale bimanual haptic interface. In *Int. Conf. on Enactive Interfaces*, pages 28–33, Pisa, Italy, November 2008.

- [59] T. Hulin, V. Schmirgel, E. Yechiam, U. E. Zimmermann, C. Preusche, and G. Pöhler. Evaluating exemplary training accelerators for programming-by-demonstration. In *IEEE Int. Symp. in Robot and Human Interactive Communication (Ro-Man)*, pages 467–472, Viareggio, Italy, September 2010.
- [60] R. Iskakov, A. Albu-Schäffer, M. Schedl, G. Hirzinger, and V. Lopota. Influence of sensor quantization on the control performance of robotics actuators. In *IEEE/RSJ Int. Conf. on Intelligent Robots and Systems (IROS)*, pages 1085–1092, San Diego, CA, USA, October 2007.
- [61] E. I. Jury. *Sampled-Data Control Systems*. John Wiley & Sons, 1958.
- [62] H. Kazerooni, T.-I. Tsay, and K. Hollerbach. A controller design framework for telerobotic systems. *IEEE Trans. on Control Systems Technology*, 1(1):50–62, March 1993.
- [63] T. A. Kern, M. Matysek, J. Rausch, A. Rettig, A. Röse, O. Meckel, and S. Sindlinger. *Engineering Haptic Devices: A Beginner’s Guide for Engineers*. Springer, 2009.
- [64] R. Konietzschke, A. Tobergte, C. Preusche, P. Tripicchio, E. Ruffaldi, S. Webel, and U. Bockholt. A multimodal training platform for minimally invasive robotic surgery. In *IEEE Int. Symp. in Robot and Human Interactive Communication (Ro-Man)*, pages 422–427, Viareggio, Italy, September 2010.
- [65] R. Kories and H. Schmidt-Walter. *Taschenbuch der Elektrotechnik: Grundlagen und Elektronik*. Harri Deutsch, 2000.
- [66] K. Kosuge, Y. Fujisawa, and T. Fukuda. Mechanical system control with man-machine-environment interactions. In *IEEE Int. Conf. on Robotics and Automation (ICRA)*, pages 239–244, May 1993.
- [67] K. J. Kuchenbecker, J. G. Park, and G. Niemeyer. Characterizing the human wrist for improved haptic interaction. In *ASME Int. Mechanical Engineering Congress and Exposition*, volume 72, pages 591–598, Washington, DC, USA, November 2003.
- [68] A. Kugi. Nichtlineare Systeme I – Vorlesung und Übung. Technical report, Johannes Kepler University Linz, 2013.
- [69] D. Lakatos, F. Petit, and P. van der Smagt. Conditioning vs. excitation time for estimating impedance parameters of the human arm. In *IEEE-RAS Int. Conf. on Humanoid Robots (Humanoids)*, volume 11, pages 636–642, Bled, Slovenia, October 2011.
- [70] D. A. Lawrence. Stability and transparency in bilateral teleoperation. *IEEE Trans. on Robotics and Automation*, 9(5):624–637, October 1993.

- [71] D. A. Lawrence and J. D. Chapel. Performance trade-offs for hand controller design. In *IEEE Int. Conf. on Robotics and Automation (ICRA)*, volume 4, pages 3211–3216, San Diego, CA, USA, May 1994.
- [72] S. J. Lederman and R. L. Klatzky. Haptic perception: A tutorial. *Attention, Perception, & Psychophysics*, 71(7):1439–1459, 2009.
- [73] S. Lee and H. Lee. Modeling, design, and evaluation of advanced teleoperator control systems with short time delay. *IEEE Trans. on Robotics and Automation*, 9(5):607–623, October 1993.
- [74] J. E. Luntz, T. R. Kurfess, and M. L. Nagurka. Explicit parameter dependency in digital control systems. In *ASME Winter Annual Meeting*, New Orleans, LA, November 1993.
- [75] H. Lutz and W. Wendt. *Taschenbuch der Regelungstechnik*. Harri Deutsch, 2005.
- [76] A. Magana. Stability analysis for a surgical simulator. Diploma thesis, Dresden University of Technology, December 2013.
- [77] S. Martin and N. Hillier. Characterisation of the Novint Falcon haptic device for application as a robot manipulator. In *Australasian Conf. on Robotics and Automation (ACRA)*, December 2009.
- [78] J. Mehling, J. E. Colgate, and M. A. Peshkin. Increasing the impedance range of a haptic display by adding electrical damping. In *IEEE World Haptics Conference (WHC)*, pages 257–262, Pisa, Italy, March 2005.
- [79] N. Miandashti and M. Tavakoli. Stability of sampled-data, delayed haptic interaction and teleoperation. In *IEEE Haptics Symp.*, pages 215–220, Houston, Texas, USA, February 2014.
- [80] B. E. Miller, J. E. Colgate, and R. A. Freeman. Guaranteed stability of haptic systems with nonlinear virtual environments. *IEEE Trans. on Robotics and Automation*, 16(6):712–719, December 2000.
- [81] M. Minsky, M. Ouh-young, O. Steele, F. Brooks Jr., and M. Behensky. Feeling and seeing: Issues in force display. *ACM SIGGRAPH Computer Graphics*, 24(2):235–243, March 1990.
- [82] S. Moberg, J. Öhr, and S. Gunnarsson. A benchmark problem for robust feedback control of a flexible manipulator. *IEEE Trans. on Control Systems Technology*, 17(6):1398–1405, November 2009.
- [83] C. A. Monje, Y. Chen, B. M. Vinagre, D. Xue, and V. Feliu-Batlle. *Fractional-order systems and controls: fundamentals and applications*. Springer, 2010.

- [84] F. A. Mussa-Ivaldi, N. Hogan, and E. Bizzi. Neural, mechanical, and geometric factors subserving arm posture in humans. *The Journal of Neuroscience*, 5(10):2732–2743, October 1985.
- [85] K. Ogata. *Modern Control Engineering*. Prentice Hall, 5th edition, 2010.
- [86] M. K. O’Malley and A. Gupta. *HCI Beyond the GUI: Design for Haptic, Speech, Olfactory, and Other Nontraditional Interfaces*, volume 1, chapter Haptic Interfaces, pages 25–73. Elsevier Inc., USA, 2008.
- [87] M. Ortega, S. Redon, and S. Coquillart. A six degree-of-freedom god-object method for haptic display of rigid bodies with surface properties. *IEEE Trans. on Visualization and Computer Graphics*, 13(3):458–469, May 2007.
- [88] R. Ortega, A. J. van der Schaft, I. Mareels, and B. Maschke. Putting energy back in control. *IEEE Control Systems Magazine*, 21(2):18–33, April 2001.
- [89] Ch. Ott, J. Artigas, and C. Preusche. Subspace-oriented energy distribution for the time domain passivity approach. In *IEEE/RSJ Int. Conf. on Intelligent Robots and Systems (IROS)*, pages 665–671, San Francisco, CA, USA, September 2011.
- [90] N. Paine and L. Sentis. A closed-form solution for selecting maximum critically damped actuator impedance parameters. *ASME Journal of Dynamic Systems, Measurement, and Control*, 137(4):041011, April 2015.
- [91] C. Preusche, T. Hulin, and G. Hirzinger. *Human Haptic Perception: Basics and Applications*, chapter 33: Haptic rendering and control. Birkhäuser Basel, 1st edition, October 2008.
- [92] D. C. Ruspini, K. Kolarov, and O. Khatib. The haptic display of complex graphical environments. In *ACM SIGGRAPH Computer Graphics*, pages 345–352, Los Angeles, CA, USA, August 1997.
- [93] J.-H. Ryu, C. Preusche, B. Hannaford, and G. Hirzinger. Time domain passivity control with reference energy behavior. *IEEE Trans. on Control Systems Technology*, 13(5):737–742, September 2005.
- [94] M. Sagardia, K. Hertkorn, T. Hulin, Simon Schätzle, R. Wolff, J. Hummel, J. Dodiya, and A. Gerndt. VR-OOS: The DLR’s virtual reality simulator for telerobotic on-orbit servicing with haptic feedback. In *IEEE Aerospace Conference*, Big Sky, Montana, USA, March 2015.
- [95] M. Sagardia, K. Hertkorn, T. Hulin, R. Wolff, J. Hummel, J. Dodiya, and A. Gerndt. An interactive virtual reality system for on-orbit servicing. In *IEEE Virtual Reality Conference*, March 2013. (Video).

- [96] M. Sagardia and T. Hulin. Fast and accurate distance, penetration, and collision queries using point-sphere trees and distance fields. In *ACM SIGGRAPH Computer Graphics*, page 83, Anaheim, CA, USA, July 2013.
- [97] M. Sagardia, T. Hulin, C. Preusche, and G. Hirzinger. Improvements of the voxmap pointshell algorithm — fast generation of haptic data structures. In *53rd IWK - Internationales Wissenschaftliches Kolloquium*, Ilmenau, Germany, September 2008.
- [98] M. Sagardia, T. Stouraitis, and J. L. e Silva. A new fast and robust collision detection and force computation algorithm applied to the physics engine Bullet: Method, integration, and evaluation. In *EuroVR*, pages 65–76, Bremen, Germany, December 2014.
- [99] S. E. Salcudean and T. D. Vlaar. On the emulation of stiff walls and static friction with a magnetically levitated input/output device. *ASME Journal of Dynamic Systems, Measurement, and Control*, 119(1):127–132, March 1997.
- [100] K. Salisbury, D. Brock, T. Massie, N. Swarup, and C. Zilles. Haptic rendering: programming touch interaction with virtual objects. In *SI3D '95: Symp. on Interactive 3D graphics*, pages 123–130, Monterey, California, United States, 1995.
- [101] K. Salisbury, F. Conti, and F. Barbagli. Haptic rendering: Introductory concepts. *IEEE Computer Graphics and Applications*, 24(2):24–32, 2004.
- [102] S. Schätzle, T. Hulin, C. Preusche, and G. Hirzinger. Evaluation of vibro-tactile feedback to the human arm. In *EuroHaptics*, pages 557–560, Paris, France, July 2006.
- [103] M. E. Schlarmann and R. L. Geiger. Relationship between amplifier settling time and pole-zero placements for second-order systems. In *IEEE Midwest Symp. on Circuits and Systems*, volume 1, pages 54–59, Lansing, MI, USA, August 2000.
- [104] V. Schmirgel, U. E. Zimmermann, T. Hulin, and C. Preusche. *beyond movement*, chapter Position Paper: Human Skills for Programming-by-Demonstration of Robots, pages 144–167. Alinea editrice s.r.l., November 2008.
- [105] V. Schmirgel, U. E. Zimmermann, E. Yechiam, T. Hulin, and C. Preusche. Comprehension of operating a robot by enactive learning: Exemplary approaches with programming-by-demonstration. In *SKILLS09 Int. Conf. on Multimodal Interfaces for Skills Transfer*, Bilbao, Spain, December 2009.
- [106] V. Schmirgel, U. E. Zimmermann, E. Yechiam, A. Telpaz, T. Hulin, and C. Preusche. *Skill Training in Multimodal Virtual Environments*, chapter Training Approaches for Improving Robot Programming-by-Demonstration Skills, pages 241–252. CRC Press, 2012.

- [107] D. Schröder. *Elektrische Antriebe - Regelung von Antriebssystemen*. Springer, 3rd edition, 2009.
- [108] R. Sepulchre, M. Janković, and P. V. Kokotović. *Constructive Nonlinear Control*. Communications and Control Engineering. Springer London, 1997.
- [109] S. M. Shinnars. *Modern Control System Theory and Design*, chapter Performance Criteria. John Wiley and Sons, Inc., 2nd edition, 1998.
- [110] N. K. Sinha. *Control Systems*. New Age International (P) Limited, 2008.
- [111] T. Sinkjaer, E. Toft, S. Andreassen, and B. C. Hornemann. Muscle stiffness in human ankle dorsiflexors: intrinsic and reflex components. *Journal of Neurophysiology*, 60(3):1110–1121, September 1988.
- [112] W. J. Staszewski and D. M. Wallace. Wavelet-based frequency response function for time-variant systems—an exploratory study. *Mechanical Systems and Signal Processing*, 1(47):35–49, 2014.
- [113] P. Staubli, T. Nef, V. Klamroth-Marganska, and R. Riener. Effects of intensive arm training with the rehabilitation robot ARMin II in chronic stroke patients: four single-cases. *Journal of NeuroEngineering and Rehabilitation*, 6(46), December 2009.
- [114] S. Stramigioli, C. Secchi, A. J. van der Schaft, and C. Fantuzzi. Sampled data systems passivity and discrete port-hamiltonian systems. *IEEE Trans. on Robotics*, 21(4):574–587, August 2005.
- [115] K. A. Stroud and D. J. Booth. *Advanced Engineering Mathematics*. Palgrave Macmillan, 5th edition, 2011.
- [116] T. Tsuji, Y. Takeda, and Y. Tanaka. Analysis of mechanical impedance in human arm movements using a virtual tennis system. *Biological Cybernetics*, 91(5):295–305, November 2004.
- [117] B. Weber, M. Sagardia, T. Hulin, and C. Preusche. Visual, vibrotactile, and force feedback of collisions in virtual environments: Effects on performance, mental workload and spatial orientation. volume 8021 of *Lecture Notes in Computer Science*, pages 241–250. Springer Berlin Heidelberg, July 2013.
- [118] B. Weber, S. Schätzle, T. Hulin, C. Preusche, and B. Deml. Evaluation of a vibrotactile feedback device for spatial guidance. In *IEEE World Haptics Conference (WHC)*, pages 349–354, Istanbul, Turkey, June 2011.
- [119] H. Weiss, T. Ortmaier, H. Maass, G. Hirzinger, and U. Kuehnappel. A virtual-reality-based haptic surgical training system. *Computer Aided Surgery*, 8(5):269–272, 2003.

- [120] R. Weller, M. Sagardia, D. Mainzer, T. Hulin, G. Zachmann, and C. Preusche. A benchmarking suite for 6-DOF real time collision response algorithms. In *ACM Symp. on Virtual Reality Software and Technology*, pages 63–70, Hong Kong, China, 2010.
- [121] J. C. Willems. Dissipative dynamical systems part II: Linear systems with quadratic supply rates. *Archive for Rational Mechanics and Analysis*, 45(5):352–393, January 1972.
- [122] J. W. Yeol, R. W. Longman, and Y. S. Ryu. On the settling time in repetitive control systems. In *Int. IFAC World Congress*, pages 12460–12467, Seoul, Korea, July 2008.
- [123] Y. Yokokohji and T. Yoshikawa. Bilateral control of master-slave manipulators for ideal kinesthetic coupling – formulation and experiment. *IEEE Trans. on Robotics and Automation*, 10(5):605–620, October 1994.
- [124] J. G. Ziegler and N. B. Nichols. Optimum settings for automatic controllers. *Transactions of ASME*, 64:759–768, November 1942.
- [125] C. B. Zilles and J. K. Salisbury. A constraint-based god-object method for haptic display. In *IEEE/RSJ Int. Conf. on Intelligent Robots and Systems (IROS)*, volume 3, pages 146–151, Pittsburgh, PA, USA, August 1995.

